

## PHASE EQUILIBRIA BY EFFECTIVE UNIFAC GROUP-CONTRIBUTION METHOD

ISAMU NAGATA \* and JITSUO KOYABU

*Department of Chemical Engineering, Kanazawa University, 2-40-20 Kodatsuno, Kanazawa, Ishikawa 920 (Japan)*

(Received 7 April 1981)

### ABSTRACT

A group-contribution method similar to the UNIFAC model is presented for the estimation of liquid phase activity coefficients. The method is based on an extension of the effective UNIQUAC equation, which represents well vapor–liquid equilibria of alcohol-saturated hydrocarbon mixtures with two parameters. Group-interaction parameters for 35 groups are obtained from experimental vapor–liquid equilibrium and solubility data. Activity coefficients in many binary and multicomponent mixtures may be estimated with good accuracy. Calculations are carried out for vapor–liquid, liquid–liquid, and solid–liquid equilibria. Both UNIFAC and effective UNIFAC seem to provide comparable results in most cases. The method, like the SIGMA of Vera, may be used for the prediction of both vapor–liquid equilibrium and excess enthalpy data for binary and ternary systems containing  $\text{CH}_2$ ,  $\text{CCOH}$ , and  $\text{CCl}$  groups.

### NOTATION

- $a_{mn}$  group interaction parameter
- $A_{mn}$  coefficient of group interaction parameter
- $B_{ij}$  second virial coefficient for  $i$ – $j$  interaction
- $B_{mn}$  coefficient of group-interaction parameter
- $G_{ji}$  effective UNIQUAC parameter defined by eqn. (5)
- $h^E$  excess enthalpy
- $\Delta h_f$  enthalpy of fusion
- $H_k$  excess enthalpy of group  $k$
- $H_k^{(i)}$  excess enthalpy of group  $k$  in pure component  $i$
- $P$  total pressure
- $P_i^s$  saturation pressure of pure component  $i$
- $q_i$  pure component area parameter of component  $i$
- $Q_k$  group area parameter for group  $k$
- $r_i$  pure component volume parameter of component  $i$
- $R_k$  group volume parameter for group  $k$
- $R$  gas constant

\* To whom correspondence should be addressed.

$T$	absolute temperature
$T_m$	melting temperature
$u_{ji}$	effective UNIQUAC binary interaction parameter
$U_{mn}$	energy parameter for m--n interaction
$v_i^L$	molar liquid volume of pure component i
$x_i$	liquid phase mole fraction of component i
$X_k$	group fraction for group k
$y_i$	vapor phase mole fraction of component i
$Z$	lattice coordination number, here equal to 10

*Greek letters*

$\gamma_i$	activity coefficient of component i
$\Gamma_k$	residual activity coefficient of group k
$\Gamma_k^{(i)}$	residual activity coefficient of group k in pure component i
$\phi_i$	fugacity coefficient of component i
$\phi_i^s$	fugacity coefficient of pure component i at its saturation pressure
$\Phi_i$	segment fraction of component i
$\nu_{ki}$	number of group of kind k in molecular species i
$\theta_i$	area fraction of component i
$\theta_k$	area fraction of group k
$\psi_{mn}$	effective UNIFAC parameter defined in eqn. (11)
$\eta_{mn}$	derivative with respect to temperature of $\psi_{mn}$

*Subscripts*

f	fusion
i, j	component
k	molecular group
m	melting in $T_m$ ; otherwise refers to molecular group
n	molecular group

*Superscripts*

C	combinatorial
L	liquid phase
R	residual
s	saturation pressure in $P_i^s$ and $\phi_i^s$ ; otherwise refers to solid phase
I, II	liquid phase

## INTRODUCTION

The group-contribution concept has been used to estimate various physico-chemical properties of pure compounds such as densities, heat capacities, and critical constants and subsequently applied to calculate activity coefficients in liquid mixtures, because the desired experimental data are often not available in the literature. The most significant approaches on the latter subject are the ASOG (Analytical Solution of Groups) method [1-3] and the UNIFAC (UNIQUAC Functional Group Activity Coefficients) method [4-10]. The UNIFAC method, in principle, is similar to the ASOG method. The UNIFAC method is based on the UNIQUAC equation [11], which contains a combinatorial term due to differences in size and shape of the

molecules in the mixtures and a residual part due to energy interaction. It has been shown that the UNIFAC method has three advantages over the ASOG method [5,10]: (1) UNIFAC has a well-defined molecular basis for establishing group sizes and shapes; (2) UNIFAC parameters are not strongly temperature-dependent for the temperature range studied; (3) UNIFAC parameters are available for many various functional groups. Skjold-Jørgensen et al. [9] have reported extensions and revisions of the UNIFAC parameter tables.

Nagata and Katoh [12] presented the effective UNIQUAC equation, which shows some advantages over the original UNIQUAC equation in representing phase equilibria for non-ideal mixtures. In this work, we report another group-contribution method based on the effective UNIQUAC equation in the calculations of vapor-liquid, liquid-liquid, and solid-liquid equilibria. The method has been tested for the prediction of vapor-liquid equilibria and excess enthalpy data for alkane, alcohol, and chloroalkane systems.

#### EFFECTIVE UNIFAC METHOD

The two-parameter effective UNIQUAC equation [12] in a multicomponent system is expressed by

$$\ln \gamma_i = \ln \gamma_i^C \text{ (combinatorial)} + \ln \gamma_i^R \text{ (residual)} \quad (1)$$

where

$$\ln \gamma_i^C = (\ln \Phi_i/x_i + 1 - \Phi_i/x_i) - (Z/2) q_i (\ln \theta_i/\theta_i + 1 - \theta_i/\theta_i) \quad (2)$$

$$\ln \gamma_i^R = 1 - \ln \left( \sum_j x_j G_{ji} \right) - \sum_k \left( \frac{x_k G_{ik}}{\sum_j x_j G_{jk}} \right) - \left( \ln \frac{\theta_i}{x_i} + 1 - \frac{\theta_i}{x_i} \right) \quad (3)$$

$$\Phi_i = r_i x_i / \sum_j r_j x_j, \quad \theta_i = q_i x_i / \sum_j q_j x_j \quad (4)$$

$$G_{ji} = (q_j/q_i) \exp[-(u_{ji} - u_{ii})/RT] \quad (5)$$

In eqns. (1)–(5),  $x_i$  is the liquid phase mole fraction,  $\Phi_i$  is the segment fraction, and  $\theta_i$  is the area fraction. Pure component structural parameters  $r_i$  and  $q_i$  are the van der Waals molecular volumes and areas [11,13]. The coordination number  $Z$  is equal to 10. The combinatorial term  $\ln \gamma_i^C$  contains only two composition variables: the average area fraction  $\theta$  and the average segment fraction  $\Phi$ . The two parameters per binary ( $u_{ji} - u_{ii}$ ) and ( $u_{ij} - u_{jj}$ ) are obtained from experimental phase equilibrium data. No ternary parameters are necessary for a multicomponent system.

The combinatorial term of the effective UNIFAC method is the same as in effective UNIQUAC. Parameters  $r_i$  and  $q_i$  are obtained by the sum of the group volume and area parameters given in Table 1 [4,5,9].

$$r_i = \sum_k \nu_{ki} R_k, \quad q_i = \sum_k \nu_{ki} Q_k \quad (6)$$

TABLE 1  
Group volume and surface-area parameters

Main group	Sub group	No	$R_k$	$Q_k$	Sample group assignment
1 "CH <sub>2</sub> "	$\begin{cases} \text{CH}_3 \\ \text{CH}_2 \\ \text{CH} \\ \text{C} \end{cases}$	1	0.9011	0.848	Butane:
		2	0.6744	0.540	2 CH <sub>3</sub> , 2 CH <sub>2</sub>
		3	0.4469	0.228	3 CH <sub>3</sub> , 1 CH
		4	0.2195	0.000	4 CH <sub>3</sub> , 1 C
2 "C = C"	$\begin{cases} \text{CH}_2 = \text{CH} \\ \text{CH} = \text{CH} \\ \text{CH} = \text{C} \\ \text{CH}_2 = \text{C} \end{cases}$	5	1.3454	1.176	1-Hexene:
		6	1.1167	0.867	2-Hexene:
		7	0.8886	0.676	2-Methyl-2-butene:
		8	1.1173	0.988	2-Methyl-1-butene:
3 "ACH"	$\begin{cases} \text{ACH} \\ \text{AC} \end{cases}$	9	0.5313	0.400	Benzene:
		10	0.3652	0.120	Styrene:
4 "ACCH <sub>2</sub> "	$\begin{cases} \text{ACCH}_3 \\ \text{ACCH}_2 \\ \text{ACCH} \end{cases}$	11	1.2663	0.968	Toluene:
		12	1.0396	0.660	Ethylbenzene:
		13	0.8121	0.348	Cumene:
5 "CCOH"	$\begin{cases} \text{CH}_2\text{CH}_2\text{OH} \\ \text{CHOHCH}_3 \\ \text{CHOHCH}_2 \\ \text{CH}_3\text{CH}_2\text{OH} \\ \text{CHCH}_2\text{OH} \end{cases}$	14	1.8788	1.664	1-Propanol:
		15	1.8780	1.660	2-Butanol:
		16	1.6513	1.352	3-Octanol:
		17	2.1055	1.972	Ethanol:
		18	1.6513	1.352	2-Methyl-1-propanol:
6	CH <sub>3</sub> OH	19	1.4311	1.432	Methanol:
7	H <sub>2</sub> O	20	0.92	1.40	Water:
8	ACOH	21	0.8952	0.680	Phenol:
		22	1.6724	1.488	Ketone group is 2nd carbon;
9 "CH <sub>2</sub> CO"	$\begin{cases} \text{CH}_3\text{CO} \\ \text{CH}_2\text{CO} \end{cases}$	23	1.4457	1.180	2-Butanone:
					Ketone group is any other carbon;
					3-Pentanone:
10	CHO	24	0.9980	0.940	Acetaldehyde:
11 "COOC"	$\begin{cases} \text{CH}_3\text{COO} \\ \text{CH}_2\text{COO} \end{cases}$	25	1.9031	1.728	Butyl acetate:
		26	1.6764	1.420	Butyl propanoate:

12	"CH <sub>2</sub> O"	$\begin{cases} \text{CH}_3\text{O} \\ \text{CH}_2\text{O} \\ \text{CH-O} \\ \text{FCH}_2\text{O} \end{cases}$	27	1.1450	1.088	Dimethyl ether:	1 CH <sub>3</sub> , 1 CH <sub>3</sub> O
			28	0.9183	0.780	Diethyl ether:	2 CH <sub>3</sub> , 1 CH <sub>2</sub> , 1 CH <sub>2</sub> O
			29	0.6908	0.468	Diisopropyl ether:	4 CH <sub>3</sub> , 1 CH, 1 CH-O
			30	0.9183	1.1	Tetrahydrofuran:	3 CH <sub>2</sub> , 1 FCH <sub>2</sub> O
13	"CNH <sub>2</sub> "	$\begin{cases} \text{CH}_3\text{NH}_2 \\ \text{CH}_2\text{NH}_2 \\ \text{CHNH}_2 \end{cases}$	31	1.5959	1.544	Methylamine:	1 CH <sub>3</sub> NH <sub>2</sub>
			32	1.3692	1.236	Propylamine:	1 CH <sub>3</sub> , 1 CH <sub>2</sub> , 1 CH <sub>2</sub> NH <sub>2</sub>
			33	1.1417	0.924	Isopropylamine:	2 CH <sub>3</sub> , 1 CHNH <sub>2</sub>
14	"CNH"	$\begin{cases} \text{CH}_3\text{NH} \\ \text{CH}_2\text{NH} \\ \text{CHNH} \end{cases}$	34	1.4337	1.244	Dimethylamine:	1 CH <sub>3</sub> , 1 CH <sub>3</sub> NH
			35	1.2070	0.936	Diethylamine:	2 CH <sub>3</sub> , 1 CH <sub>2</sub> , 1 CH <sub>2</sub> NH
			36	0.9795	0.624	Diisopropylamine:	4 CH <sub>3</sub> , 1 CH, 1 CHNH
15		ACNH <sub>2</sub>	37	3.7165	2.816	Aniline:	1 ACNH <sub>2</sub>
16	"CCN"	$\begin{cases} \text{CH}_3\text{CN} \\ \text{CH}_2\text{CN} \end{cases}$	38	1.8701	1.724	Acetonitrile:	1 CH <sub>3</sub> CN
			39	1.6434	1.416	Propionitrile:	1 CH <sub>3</sub> , 1 CH <sub>2</sub> CN
17	"COOH"	$\begin{cases} \text{COOH} \\ \text{HCOOH} \end{cases}$	40	1.3013	1.224	Acetic acid:	1 CH <sub>3</sub> , 1 COOH
			41	1.5280	1.532	Formic acid:	1 HCOOH
18	"CCl"	$\begin{cases} \text{CH}_2\text{Cl} \\ \text{CHCl} \\ \text{CCl} \end{cases}$	42	1.4654	1.264	1-Chlorobutane:	1 CH <sub>3</sub> , 2 CH <sub>2</sub> , 1 CH <sub>2</sub> Cl
			43	1.2380	0.952	2-Chloropropane:	2 CH <sub>3</sub> , 1 CHCl
			44	1.0060	0.724	2-Chloro-2-methylpropane:	3 CH <sub>3</sub> , 1 CCl
19	"CCl <sub>2</sub> "	$\begin{cases} \text{CH}_2\text{Cl}_2 \\ \text{CHCl}_2 \\ \text{CCl}_2 \end{cases}$	45	2.2564	1.988	Dichloromethane:	1 CH <sub>2</sub> Cl <sub>2</sub>
			46	2.0606	1.684	1,1-Dichloroethane:	1 CH <sub>3</sub> , 1 CHCl <sub>2</sub>
			47	1.8016	1.448	2,2-Dichloropropane:	2 CH <sub>3</sub> , 1 CCl <sub>2</sub>
20	"CCl <sub>3</sub> "	$\begin{cases} \text{CHCl}_3 \\ \text{CCl}_3 \end{cases}$	48	2.8700	2.410	Chloroform:	1 CHCl <sub>3</sub>
			49	2.6401	2.184	1,1,1-Trichloroethane:	1 CH <sub>3</sub> , 1 CCl <sub>3</sub>
21		CCl <sub>4</sub>	50	3.3900	2.910	Tetrachloromethane:	1 CCl <sub>4</sub>
22		ACCl	51	1.1562	0.844	Chlorobenzene:	5 ACH, 1 ACCl
23	"CNO <sub>2</sub> "	$\begin{cases} \text{CH}_3\text{NO}_2 \\ \text{CH}_2\text{NO}_2 \\ \text{CHNO}_2 \\ \text{ACNO}_2 \\ \text{CS}_2 \\ \text{CH}_3\text{N} \\ \text{CH}_2\text{N} \\ \text{HCOO} \\ \text{I} \\ \text{Br} \end{cases}$	52	2.0086	1.868	Nitromethane:	1 CH <sub>3</sub> NO <sub>2</sub>
			53	1.7818	1.560	1-Nitropropane:	1 CH <sub>3</sub> , 1 CH <sub>2</sub> , 1 CH <sub>2</sub> NO <sub>2</sub>
			54	1.5544	1.248	2-Nitropropane:	2 CH <sub>3</sub> , 1 CHNO <sub>2</sub>
			55	1.4199	1.104	Nitrobenzene:	5 ACH, 1 ACNO <sub>2</sub>
			56	2.057	1.65	Carbon disulfide:	1 CS <sub>2</sub>
			57	1.1865	0.940	Trimethylamine:	2 CH <sub>3</sub> , 1 CH <sub>3</sub> N
			58	0.9597	0.932	Triethylamine:	3 CH <sub>3</sub> , 2 CH <sub>2</sub> , 1 CH <sub>2</sub> N
			59	1.242	1.188	Ethyl formate:	1 CH <sub>3</sub> , 1 CH <sub>2</sub> , 1 HCOO
			60	1.264	0.992	Iodoethane:	1 CH <sub>3</sub> , 1 CH <sub>2</sub> , 1 I
			61	0.9492	0.832	Bromomethane:	1 CH <sub>3</sub> , 1 Br
						Bromobenzene:	5 ACH, 1 AC, 1 Br

TABLE 1 (continued)

Main group	Sub group	No	$R_k$	$Q_k$	Sample group assignment
30	CH <sub>3</sub> SH	62	1.877	1.676	1 CH <sub>3</sub> SH
31	Furfural	63	3.168	2.484	1 Furfural
32	$\left\{ \begin{array}{l} C_5H_5N \\ C_5H_4N \\ C_5H_3N \end{array} \right.$	64	2.9993	2.113	1 C <sub>5</sub> H <sub>5</sub> N
"Pyridine"		65	2.8332	1.833	1 CH <sub>3</sub> , 1 C <sub>5</sub> H <sub>4</sub> N
		66	2.667	1.553	2 CH <sub>3</sub> , 1 C <sub>5</sub> H <sub>3</sub> N
33	(CH <sub>2</sub> OH) <sub>2</sub>	67	2.4088	2.248	1 (CH <sub>2</sub> OH) <sub>2</sub>
34	HCON(CH <sub>3</sub> ) <sub>2</sub>	68	3.0856	2.736	1 HCON(CH <sub>3</sub> ) <sub>2</sub>
35	(CH <sub>3</sub> ) <sub>2</sub> SO	69	2.8266	2.472	1 (CH <sub>3</sub> ) <sub>2</sub> SO
					Methanethiol
					Furfural:
					Pyridine:
					3-Methylpyridine:
					2,3-Dimethylpyridine
					1,2-Ethanediol:
					Dimethylformamide:
					Dimethylsulfoxide:

where  $\nu_{ki}$  is the number of groups of type  $k$  in molecule  $i$  and is always an integer.  $\ln \gamma_i^R$  is given by

$$\ln \gamma_i^R = \sum_k \nu_{ki} (\ln \Gamma_k - \ln \Gamma_k^{(i)}) - \left( \ln \frac{\theta_i}{x_i} + 1 - \frac{\theta_i}{x_i} \right) \quad (7)$$

where  $\Gamma_k$  is the group residual activity coefficient and  $\Gamma_k^{(i)}$  is the residual activity coefficient of group  $k$  in a reference solution containing only molecules of type  $i$ .  $\ln \Gamma_k$  and  $\ln \Gamma_k^{(i)}$  are calculated from the equation

$$\ln \Gamma_k = 1 - \ln \left( \sum_m X_m \Psi_{mk} \right) - \sum_m \left( \frac{X_m \Psi_{km}}{\sum_n X_n \Psi_{nm}} \right) \quad (8)$$

using the group fractions  $X_m$  in the mixture for  $\ln \Gamma_k$  and the group fractions  $X_m^{(i)}$  in pure component  $i$  for  $\ln \Gamma_k^{(i)}$ . The mole fraction of group  $k$  in the mixture is given by

$$X_m = \frac{\sum_j \nu_{mj} x_j}{\sum_j \sum_n \nu_{nj} x_j} \quad (9)$$

For pure component  $i$ , eqn. (9) reduces to

$$X_m^{(i)} = \nu_{mi} / \sum_n \nu_{ni} \quad (10)$$

The group interaction parameter  $\Psi_{mn}$  is given by

$$\Psi_{mn} = (Q_m/Q_n) \exp[-(U_{mn} - U_{nn})/RT] = (Q_m/Q_n) \exp(-a_{mn}/T) \quad (11)$$

where  $U_{mn}$  is the energy of interaction between groups  $m$  and  $n$ . The group interaction parameters  $a_{mn}$  and  $a_{nm}$  ( $a_{mn} \neq a_{nm}$ ) must be systematically evaluated from the existing literature concerning phase equilibrium data [14–16] as shown in Table 2.

## BASIC PHASE EQUILIBRIUM EQUATIONS

We can summarize the following equations for three-phase equilibria [17].

Vapor–liquid equilibria under normal pressures are calculated by

$$\phi_i y_i P = x_i \gamma_i \phi_i^s P_i^s \exp[v_i^L (P - P_i^s)/RT] \quad (12)$$

where  $y_i$  is the vapor phase mole fraction,  $\phi$  is the vapor phase fugacity coefficient,  $v_i^L$  is the molar liquid volume,  $P_i^s$  is the saturation pressure, and  $P$  is the total pressure.

The fugacity coefficients of pure components and components in a mixture are calculated from the second virial coefficients  $B_{ij}$ .

$$\ln \phi_i = (P/RT) \left( 2 \sum_j y_j B_{ij} - \sum_i \sum_j y_i y_j B_{ij} \right) \quad (13)$$

The pure component and cross-virial coefficients are calculated from the correlation of Hayden and O'Connell [18].

TABLE 2

Effective UNIFAC group interaction parameters  $\sigma_{mm}$ , K

	1	2	3	4	5	6	7	8	9
	CH <sub>2</sub>	C=C	ACH	ACCH <sub>2</sub>	CCOH	CH <sub>3</sub> OH	H <sub>2</sub> O	ACOH	CH <sub>2</sub> CO
1	CH <sub>2</sub>	0	126.7	176.2	963.6	1026.	1733.	1303.	487.9
2	C=C	2000.	660.8	4964.	10100.	1528.	5008.	357.6	386.7
3	ACH	-107.1	0	107.7	552.5	721.9	1198.	966.6	119.8
4	ACCH <sub>2</sub>	-87.66	31.09	0	747.1	580.3	5319.	646.5	2887.
5	CCOH	184.7	249.6	79.89	0	247.1	407.4	-152.0	246.8
6	CH <sub>3</sub> OH	94.54	170.4	81.55	-236.7	0	-150.6	0	112.2
7	H <sub>2</sub> O	456.8	327.8	358.7	-214.3	255.1	0	-308.5	-305.5
8	ACOH	6091.	-56.41	-120.2	-649.4	7468.	0	0	0
9	CH <sub>2</sub> CO	243.0	389.6	239.8	4.681	89.10	674.5	0	0
10	CHO	473.4				961.3	656.0		24.82
11	COOC	298.4	-330.3	477.8	156.6	272.0	744.0	-9.114	292.9
12	CH <sub>2</sub> O	66.80	125.6	158.7	1190.	230.4	933.0		179.1
13	CNH <sub>2</sub>	74.20	2335.	140.4	-330.2	-479.8	-545.9		
14	CNH	40.09	1145.	147.8	-237.8	-533.2	-624.1		
15	ACNH <sub>2</sub>	337.8	479.0	396.1	190.6	327.3	-101.1		-250.4
16	CCN	164.5	441.3	239.4	136.7	498.5	353.0		-5.491
17	COOH	240.9	3780.	187.6	220.8	921.8	-433.9		-164.1
18	CCl	141.9	32.64	334.8	159.5	691.2	1084.		77.34
19	CCl <sub>2</sub>	154.1	216.4	705.1	424.0	789.8	5010.		53.88
20	CCl <sub>3</sub>	222.8	320.9	511.1	167.9	783.5	5141.		91.44
21	CCl <sub>4</sub>	470.6	594.0	630.8	404.0	1119.	8865.	1720.	421.6
22	ACCl	-151.8	-84.39	-74.73	-64.02	1307.	1471.		6052.
23	CNO <sub>2</sub>	199.2	95.96	255.3	65.97	313.0	1431.		-118.2
24	ACNO <sub>2</sub>	457.5		99.36		5716.	5716.		442.9
25	CS <sub>2</sub>	151.7	4.520	251.0	-153.2	1214.	2927.		130.2
26	(C) <sub>3</sub> N	150.1	150.0	142.4		543.3	-792.9		-166.1
27	HCOO	329.1		252.4	2.197	209.4			-206.7
28	I	-4.810		191.7		355.4			204.3
29	Br	-69.69		-3.001	145.2	447.3			423.4
30	CH <sub>3</sub> SH	113.2		323.3		535.0			387.5
31	Furfural	271.6		529.3	403.5	4423.	344.1		117.7
32	Pyridine	180.7		280.4	281.8	548.1	-332.4	-231.7	
33	DOH	473.8		429.6	5574	255.5		1798.	
34	DMFA	233.9		678.0	608.3	353.6	-119.7		
35	DMSO	320.0	668.4	304.3	-105.8	-59.19	-334.9		

	10	11	12	13	14	15	16	17	18
	CHO	COOC	CH <sub>2</sub> O	CNH <sub>2</sub>	CNH	ACNH <sub>2</sub>	CCN	COOH	CCl
1	476.6	364.9	193.6	407.3	302.6	517.1	927.8	727.6	67.58
2		391.8	300.7	297.8	277.7	717.9	931.6	20 080.	459.7
3		-245.7	-66.28	134.9	43.93	-5.894	101.9	566.4	-337.2
4		602.9	-156.3		135.8	3847.	4874.	761.5	-124.7
5		275.4	400.4	-107.5	-7.708	88.73	352.3	777.4	6073.
6	-361.8	41.43	-61.09	44.35	87.55	-82.01	-6.257	-300.0	21.84
7	-207.7	-356.4	-280.5	154.6	334.6	963.5	180.8	412.6	450.0
8		-116.6							
9	24.17	-190.1	-27.85			5421.	-20.10	290.5	-28.42
10	0								3009.
11		0	61.73		101.5		26.28	8,026	
12		69.60	0		-199.1		135.9	684.1	41.58
13				0	-33.52				
14		-23.17	939.7	118.2	0				
15						0	-149.0	861.8	124.0
16		20.65	60.55			476.0	0	0	0
17		35.50	-305.3				-487.9	623.5	61.79
18	-72.09		354.3					273.5	-2.826
19		-35.88	-141.5				106.0	945.0	
20		65.74	-132.6		262.2	383.3	740.0		
21		248.6	-42.20		-15.66	1029.	7255.		
22		-18.95		628.5			-125.4		1299.
23			219.7						
24						-334.7			
25		454.8	168.2				869.3		18.75
26				-51.29			414.5		
27		-18.87						-343.2	
28		41.60	797.6						
29			-192.0						
30			152.5	-45.09			186.0		-0.5514
31		2.926							
32			26.42						
33			286.9			196.2	306.2		
34									
35		82.90	87.21			294.6			

TABLE 2 (continued)

	19	20	21	22	23	24	25	26	27
	CCl <sub>2</sub>	CCl <sub>3</sub>	CCl <sub>4</sub>	ACCl	CNO <sub>2</sub>	ACNO <sub>2</sub>	CS <sub>2</sub>	(C) <sub>3</sub> N	HCOO
1	CH <sub>2</sub>	41.16	-31.00	-439.3	807.3	59.40	-53.53	-27.01	543.1
2	C=C	297.4	89.02	-430.3	1047.	4252.	185.4	413.6	
3	ACH	-722.7	-543.1	-627.9	153.9	424.2	-100.3	-134.0	177.0
4	ACCH <sub>2</sub>	-31.37	207.2	-397.3	4121.	46.78	148.8		1293.
5	CCOH	-162.4	-115.0	117.1	285.1	285.1	300.1	-410.6	475.9
6	CH <sub>3</sub> OH	-36.92	-137.3	125.5	38.77	241.3	465.7	-625.7	254.2
7	H <sub>2</sub> O	1025.	1030.	1739.	525.5	-70.28	623.9	624.5	
8	ACOH			5136.					
9	CH <sub>2</sub> CO	-163.4	-204.2	4522.	63.16	101.7	1108.		-75.00
10	CHO								
11	COOC	-51.66	-212.2	4685.	295.9		387.7		40.50
12	CH <sub>2</sub> O	2441.	5264.	-91.82	-208.3		102.1		
13	CNH <sub>2</sub>				-14.33			-38.07	
14	CNH			-48.11	167.1				
15	ACNH <sub>2</sub>			195.0	171.4	417.7			
16	CCN	-1.076		125.9	152.5		576.8	-153.9	
17	COOH	2155.		6646.					691.6
18	CCI	-41.93	89.43	110.4			3523.		
19	CCl <sub>2</sub>	0		42.50				-274.3	
20	CCl <sub>3</sub>		0	-52.19			220.6	-401.1	155.6
21	CCl <sub>4</sub>	98.95	107.1	0	833.2	1515.	147.2	-9.331	
22	ACCl			-653.9	0			1554.	
23	CNO <sub>2</sub>			288.1	0				
24	ACNO <sub>2</sub>			170.0	0	0			
25	CS <sub>2</sub>		-62.20	-65.09	834.7		0		
26	(C) <sub>3</sub> N	3016.	-302.3	382.0	8616.			0	
27	HCOO		-57.81		0				
28	I	51.06	32.56	-103.5	157.5				0
29	Br			3497.	201.8				
30	CH <sub>3</sub> SH				136.5				355.7
31	Furfural		34.63	144.1					
32	Pyridine	-149.2	-294.4	-277.3					
33	DOH								
34	DMFA								
35	DMSO	-219.5	-426.4	108.1					
					1589.				

	28	29	30	31	32	33	34	35
I	I	Br	CH <sub>3</sub> SH	Furfural	Pyridine	DOH	DMFA	DMSO
1	CH <sub>2</sub>	422.6	164.1	779.9	357.2	181.8	657.1	1577.
2	C=C							1102.
3	ACH	115.9	-284.9	-364.3	38.72	549.7	-644.9	252.9
4	ACCH <sub>2</sub>	-86.31	477.0	477.0	-146.6	1122.	130.4	
5	CCOH	278.2		79.32	-14.51	-172.5	77.53	-210.4
6	CH <sub>3</sub> OH		149.4		152.9		-465.6	-265.9
7	H <sub>2</sub> O			230.7	932.0		125.8	-268.7
8	ACOH				-680.9	-866.8		
9	CH <sub>2</sub> CO	292.4	-23.60	-267.6			-309.7	36.54
10	CHO							
11	COOC	164.0		14.79				194.1
12	CH <sub>2</sub> O	-183.7	-141.4			4540.	-80.94	188.8
13	CNH <sub>2</sub>		179.9					
14	CNH							
15	ACNH <sub>2</sub>					384.0		-147.5
16	CCN		74.72		-139.7			
17	COOH							
18	CCl		41.37					
19	CCl <sub>2</sub>	111.9			-50.75			166.3
20	CCl <sub>3</sub>	128.4		-81.10	-15.32			171.3
21	CCl <sub>4</sub>	480.6		369.7	451.8		837.6	710.7
22	ACCl	309.2						
		119.1						
23	CNO <sub>2</sub>	76.47				782.7		
24	ACNO <sub>2</sub>							
25	CS <sub>2</sub>	358.1						
26	(C) <sub>3</sub> N							
27	HCOO		41.15					
28	I	0						
29	Br	0						
30	CH <sub>3</sub> SH		0			-41.99		
31	Furfural			0				
32	Pyridine				0			
33	DOH		142.3			0	-244.7	-406.1
34	DMFA					385.1	0	161.9
35	DMSO					81.65	-98.33	0

Liquid-liquid equilibrium compositions between two liquid phases (I and II) can be calculated by [19]

$$(x_i \gamma_i)^I = (x_i \gamma_i)^{II} \quad (14)$$

The solubility of a solid (component 2) in a liquid solvent (component 1) is calculated by eqn. (15) when there is no solubility of component 1.

$$f_{\text{pure } 2}^S = \gamma_2 x_2 f_{\text{pure } 2}^L \quad (15)$$

The ratio  $(f^S/f^L)_{\text{pure } 2}$  is given elsewhere [17] and its simplified form, which neglects terms containing specific heat difference between liquid and solid, is

$$\ln(f^S/f^L)_{\text{pure } 2} = (\Delta h_{f,2}/RT) [T/T_{m,2} - 1] \quad (16)$$

where  $\Delta h_{f,2}$  is the enthalpy of fusion,  $T_{m,2}$  is the melting temperature of pure component 2 and  $T$  is the system temperature. The solubility  $x_2$  can be calculated if the activity coefficient  $\gamma_2$  is estimated by a group-contribution method. We must use the approximation  $\gamma_2 = 1$  to obtain the ideal solubility.

## RESULTS

The effective UNIFAC method can predict a better fit of vapor-liquid equilibria for alcohol-saturated hydrocarbon systems than the UNIFAC method as shown in Table 3. Figures 1 and 2 show typical examples to indi-

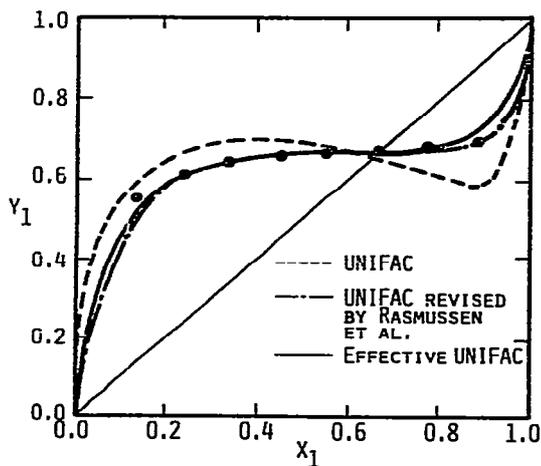


Fig. 1. Vapor-liquid equilibria for *n*-hexane (1)-ethanol (2) at 60°C. ●, Data from ref. 21.

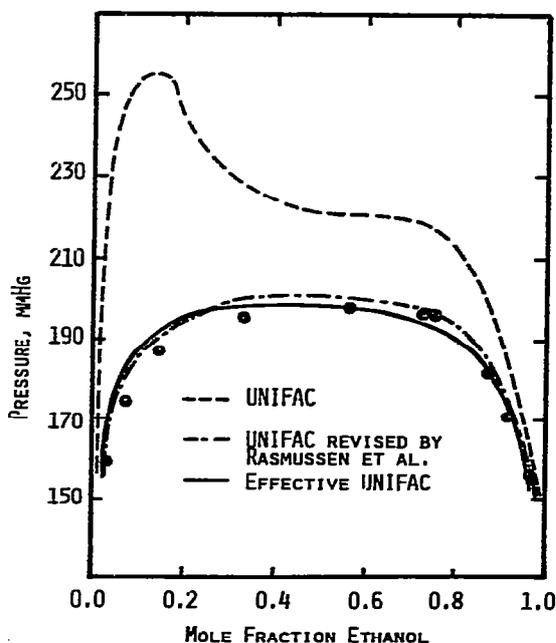


Fig. 2. Vapor-liquid equilibria for ethanol-*n*-heptane at 40°C. ●, Data from ref. 22.

TABLE 3

Prediction of vapor-liquid equilibria for binary alcohol-hydrocarbon systems from group-contribution methods

System (component 1— component 2)	Temp. (°C)	No. of data points	Root-mean square deviation (× 1000)				Ref.
			Relative press.		Vapor mole fraction		
			I a	II b	I	II	
Methanol- <i>n</i> -hexane	60	23	75	37			20
Ethanol- <i>n</i> -hexane	60	8	153	45	56	18	21
Ethanol- <i>n</i> -heptane	40	10	225	19	89	24	22
Ethanol- <i>n</i> -octane	45	17	242	32	55	16	23
	55	19	259	35	60	21	23
	65	18	246	33	57	14	23
	75	19	256	36	70	18	23
Ethanol-isooctane	40	18	206	43	86	31	22
1-Propanol- <i>n</i> -hexane	45	5	26	57	11	9	24
1-Propanol- <i>n</i> -heptane	30	9	29	52			25
	60	13	28	53			25
1-Propanol- <i>n</i> -decane	90	11	104	42	10	7	22
1-Butanol- <i>n</i> -decane	100	19	33	35	18	18	26
2-Propanol- <i>n</i> -heptane	30	11	45	49			25
2-Propanol-isooctane	45	20	55	23	37	21	27

a I = UNIFAC.

b II = Effective UNIFAC.

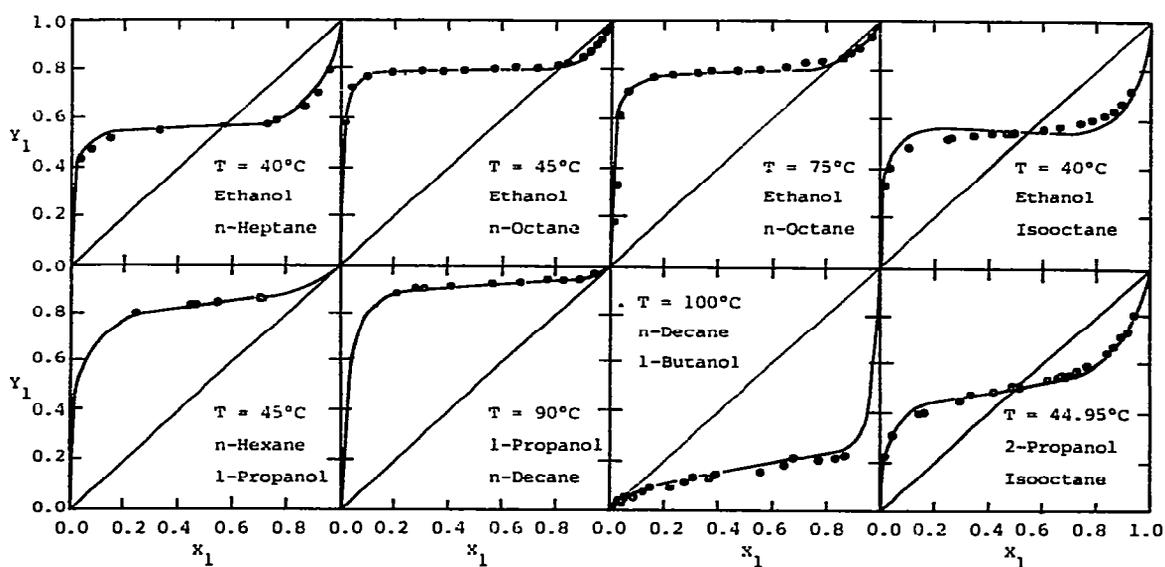


Fig. 3. Vapor-liquid equilibria for binary alcohol-hydrocarbon systems [22-24,26,27].

TABLE 4

Experimental and calculated activity coefficients for binary systems

System (component 1—component 2)	$T$ (°C)	$x_1$	$\gamma_1$ (exptl.)	$\gamma_1$ (calcd.)	Ref.
Methanol— <i>n</i> -hexane	60	0.045	13.50	11.88	20
<i>n</i> -Hexane—methanol	60	0.0513	14.90	13.60	
Ethanol— <i>n</i> -octane	45	0.0206	16.36	16.30	23
<i>n</i> -Octane—ethanol	45	0.0985	6.679	6.223	
1-Propanol—benzene	45	0.0972	5.010	4.881	28
Benzene—1-propanol	45	0.0807	3.738	3.470	
Methanol—benzene	35	0.0242	11.08	11.34	29
Benzene—methanol	35	0.0803	4.977	5.204	
Methanol—toluene	70.25	0.130	4.574	4.454	30
Toluene—methanol	63.62	0.073	5.714	5.748	
<i>n</i> -Octane—phenol	132.41	0.250	2.789	2.731	31
Phenol— <i>n</i> -octane	125.59	0.014	8.730	8.730	
<i>n</i> -Heptane—1,4-dioxane	80	0.049	3.172	3.317	32
1,4-Dioxane— <i>n</i> -heptane	80	0.023	2.464	2.484	
1-Octene—1,4-dioxane	80	0.063	2.393	2.457	32
1,4-Dioxane—1-octene	80	0.120	1.742	1.828	
<i>n</i> -Pentane—acetone	45	0.105	3.500	3.577	33
Acetone— <i>n</i> -pentane	45	0.094	3.861	3.568	
1-Hexene—5-nonanone	60	0.	1.287	1.283	34
5-Nonanone—1-hexene	60	0.	1.633	1.564	
Benzene—dipropyl ether	70	0.0751	1.052	1.050	35
Dipropyl ether—benzene	70	0.0350	1.099	1.147	
Benzene—acetone	45	0.0916	1.409	1.327	36
Acetone—benzene	45	0.0470	1.531	1.474	
Toluene—acetone	45	0.1974	1.403	1.400	37
Acetone—toluene	45	0.0688	1.656	1.583	
Methyl acetate—cyclohexane	35	0.111	3.167	3.026	38
Cyclohexane—methyl acetate	35	0.079	3.641	3.409	
Methyl acetate—benzene	50	0.080	1.294	1.290	38
Benzene—methyl acetate	50	0.073	1.321	1.352	
Cyclohexane—propionaldehyde	45	0.0090	4.436	4.411	39
Propionaldehyde—cyclohexane	45	0.0093	3.624	3.599	
Hexylamine— <i>n</i> -hexane	60	0.123	1.546	1.504	40
<i>n</i> -Hexane—hexylamine	60	0.094	1.486	1.443	
Dimethylamine— <i>n</i> -hexane	20	0.0498	2.003	1.871	41
<i>n</i> -Hexane—dimethylamine	20	0.0440	2.469	2.468	
Aniline—methylcyclohexane	100	0.0976	4.318	5.430	42
Methylcyclohexane—aniline	100	0.0763	4.979	5.049	
<i>n</i> -Butylamine—benzene	70	0.0720	1.185	1.190	43
Benzene— <i>n</i> -butylamine	70	0.1135	1.130	1.127	
Acetonitrile—benzene	45	0.0940	2.300	2.130	44
Benzene—acetonitrile	45	0.0427	2.669	2.608	
Nitromethane—benzene	45	0.0445	2.968	2.763	45
Benzene—nitromethane	45	0.0399	3.072	2.897	
<i>n</i> -Hexane—chloroform	35	0.0991	1.622	1.691	46
Chloroform— <i>n</i> -hexane	35	0.1005	1.415	1.444	
Carbon disulfide—benzene	25	0.0581	1.343	1.325	47
Benzene—carbon disulfide	25	0.0211	1.700	1.637	
Water—benzene	25	0.0027	366.6	366.6	15
Benzene—water	25	0.0004	2427.	2430.	
Water—1-propanol	90	0.162	2.674	2.801	22

TABLE 4 (continued)

System (component 1—component 2)	$T$ (°C)	$x_1$	$\gamma_1$ (exptl.)	$\gamma_1$ (calcd.)	Ref.
1-Propanol—water	90	0.111	4.663	4.753	
Water—2-propanol	45	0.1	2.985	3.135	48
2-Propanol—water	45	0.1	4.708	5.226	
Water—acetic acid	113.5	0.099	1.745	1.620	49
Acetic acid—water	100.1	0.015	2.860	2.911	
Water—acetonitrile	60	0.0529	5.231	5.698	50
Acetonitrile—water	60	0.0654	7.335	6.825	
Butyl acetate—phenol	176.6	0.1300	0.606	0.606	51
Phenol—butyl acetate	128.6	0.0500	0.558	0.543	
3-Pentanone—acetic acid	70	0.0314	1.434	1.517	52
Acetic acid—3-pentanone	70	0.0890	1.525	1.432	
Acetone—chloroform	62.06	0.0563	0.579	0.534	53
Chloroform—acetone	58.77	0.1609	0.662	0.650	
Chloroform—methanol	61.9	0.095	2.292	2.384	54
Methanol—chloroform	58.9	0.030	5.345	5.376	
Diethyl ether—methanol	55.78	0.0390	3.118	3.022	55
Methanol—diethyl ether	32.48	0.1716	2.413	2.475	
Methanol—water	93.5	0.040	2.093	2.011	56
Water—methanol	65.0	0.050	1.670	1.632	

cate the predictive ability of both methods. Figure 3 illustrates experimental and calculated vapor mole fractions for some alcohol—hydrocarbon systems. Table 4 presents typical experimental and calculated activity coefficients in the dilute regions for various binary systems, demonstrating that the effective UNIFAC method is able to represent a wide range of mixtures with few group parameters. Table 5 shows some of the predicted results for the chloroform—methanol—ethyl acetate system which exhibits positive and negative deviations from the Raoult law. Table 6 compares predictions obtained by the two methods for selected ternary systems. For the ethyl acetate—ethanol—water system, the effective UNIFAC method shows considerable improvement.

Prediction of liquid—liquid equilibria has been carried out for four ternary systems having a plait point. The data are obtained from Landolt—Börnstein [60]. The agreement between predicted and experimental solubility curves are quantitatively good for the water—propionic acid—*n*-octane and cyclohexane—ethanol—water systems at 25°C as shown in Figs. 4 and 5. However, the predictions agree qualitatively with experimental values for the toluene—acetic acid—water and water—2-propanol—chloroform systems at 25°C (Figs. 6 and 7). We may state that the prediction of liquid—liquid equilibria using group-contribution methods with parameters obtained from vapor—liquid equilibrium data will give results which agree qualitatively with experiment [5]. To predict liquid—liquid equilibria well by the present method, we should prepare a separate effective UNIFAC group interaction parameter table for liquid—liquid equilibria, which are derived from published binary and ternary liquid—liquid equilibrium data, and work on such a table is currently under way.

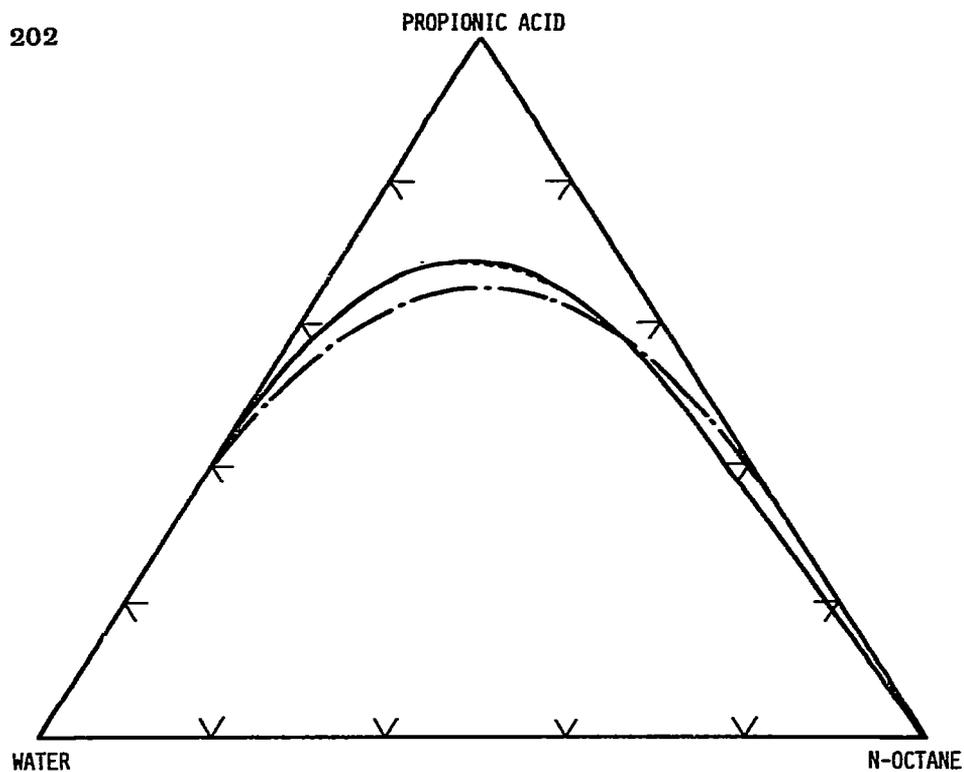


Fig. 4. Liquid-liquid equilibria for water-propionic acid-*n*-octane at 25°C [60]. ---, Effective UNIFAC; ·-·-·, UNIFAC; —, experimental.

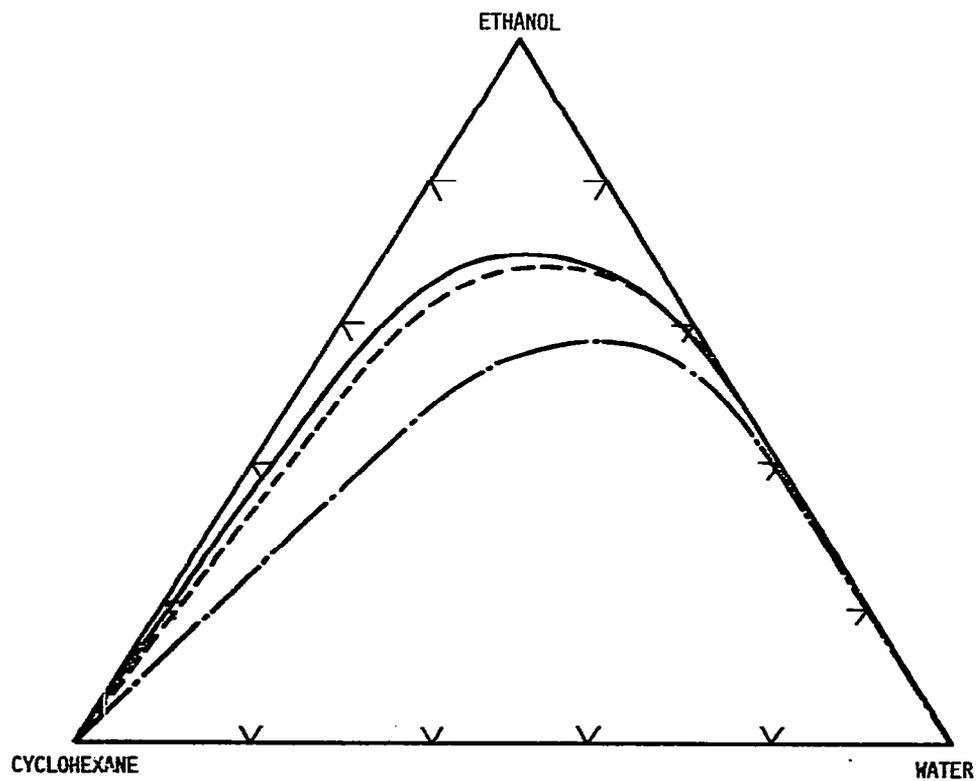


Fig. 5. Liquid-liquid equilibria for cyclohexane-ethanol-water at 25°C [60]. ---, Effective UNIFAC, ·-·-·, UNIFAC; —, experimental.

**TABLE 5**  
**Experimental and calculated activity coefficients for the chloroform(1)-methano(2)-ethyl acetate(3) system at one atmosphere [54]**

$x_1$	$x_2$	$\gamma_1$		$\gamma_2$		$\gamma_3$				
		Exptl.	I <sup>a</sup>	II <sup>b</sup>	Exptl.	I	II	Exptl.	I	II
0.122	0.539	1.01	1.14	1.13	1.28	1.27	1.27	1.27	1.28	1.27
0.116	0.179	0.637	0.695	0.686	1.94	2.10	1.02	2.05	1.01	1.01
0.120	0.637	1.24	1.36	1.34	1.15	1.18	1.39	1.16	1.43	1.40
0.345	0.465	1.24	1.26	1.24	1.42	1.39	0.812	1.38	0.989	0.971
0.454	0.325	1.12	1.11	1.09	1.70	1.76	0.774	1.73	0.812	0.811
0.597	0.077	0.896	0.904	0.895	3.10	3.51	0.673	3.39	0.738	0.734
0.058	0.634	1.11	1.26	1.24	1.16	1.16	1.44	1.15	1.48	1.45
0.553	0.082	0.939	0.938	0.931	3.19	3.57	0.573	3.43	0.672	0.673

<sup>a</sup> I = UNIFAC.

<sup>b</sup> II = Effective UNIFAC.

TABLE 6

Prediction of vapor-liquid equilibria for ternary systems from group-contribution methods

System	Temp. or press.	No. of data points	Root-mean square deviation ( $\times 1000$ )				Ref.
			Relative press.		Vapor mole fraction		
			I <sup>a</sup>	II <sup>b</sup>	I	II	
Ethanol— 2-butanone— benzene	25°C	33	44	29	24 11 25	16 14 28	57
Acetonitrile— benzene— <i>n</i> -heptane	45°C	51	44	43	25 10 20	22 13 13	58
Ethyl acetate— ethanol— water	40°C	9	213	103	111 61 100	22 26 24	59
Ethyl acetate ethanol— water	70°C	9	215	43	98 60 82	10 18 15	59
Chloroform— methanol— ethyl acetate	1 atm	72	24	17	11 14 12	11 12 11	54

<sup>a</sup> I = UNIFAC.<sup>b</sup> II = Effective UNIFAC.

TABLE 7

Solubility of naphthalene, anthracene, and phenanthrene in solvents

Solvent	Temp. (°C)	Solubility (mole%)			Ref.
		I <sup>a</sup>	II <sup>b</sup>	Exptl.	
Naphthalene—methanol	40	4.8	6.7	4.4	65
Naphthalene—ethanol	40	5.4	10.1	7.3	62
Naphthalene—1-butanol	40	11.1	15.0	11.6	65
Naphthalene—acetone	40	35.8	37.0	37.8	65
Naphthalene—chloroform	40	47.0	43.0	47.3	66
Anthracene—acetone	20	0.25	0.91	0.31	67
Anthracene—chloroform	20	1.82	1.86	0.94	67
Anthracene—carbon tetrachloride	20	0.53	0.42	0.41	67
Anthracene—cyclohexane	20	0.31	0.29	0.12	67
Anthracene—methanol	20	0.03	0.12	0.02	67
Anthracene—aniline	20	0.27	0.30	0.35	67
Phenanthrene—acetone	20	9.7	14.0	14.5	68
Phenanthrene—chloroform	20	26.4	19.4	23.8	68
Phenanthrene—carbon tetrachloride	20	15.8	14.0	14.5	68
Phenanthrene—carbon disulfide	20	18.5	17.2	23.5	68

<sup>a</sup> I = UNIFAC.<sup>b</sup> II = Effective UNIFAC.

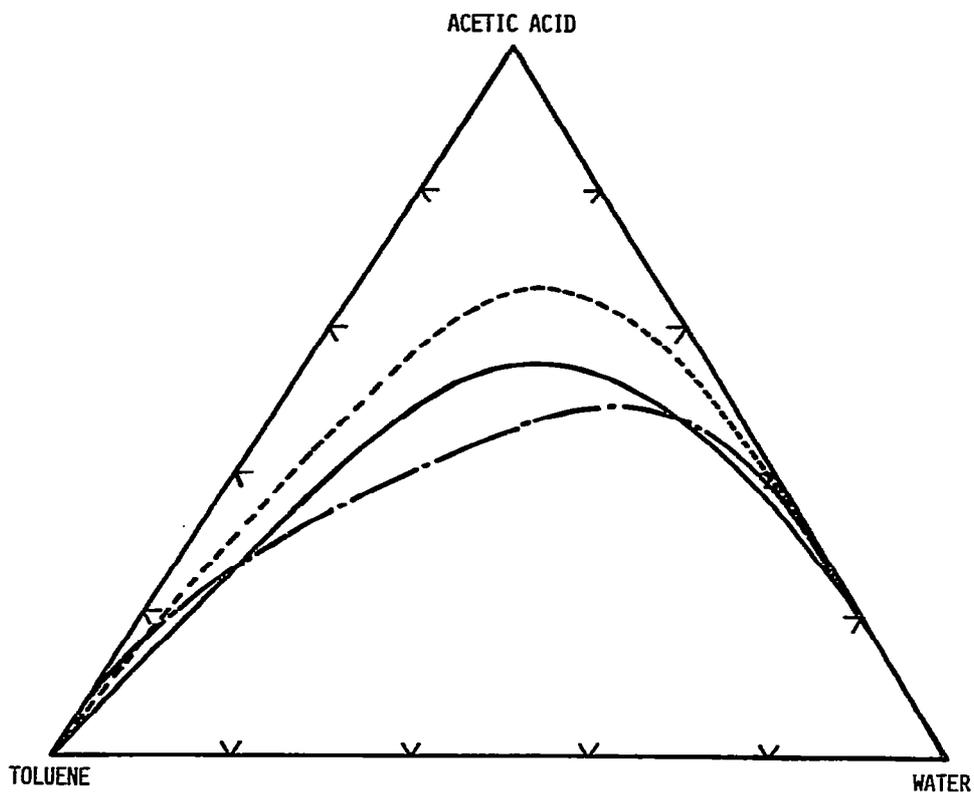


Fig. 6. Liquid-liquid equilibria for toluene-acetic acid-water at 25°C [60]. ---, Effective UNIFAC; ·-·-·, UNIFAC; —, experimental.

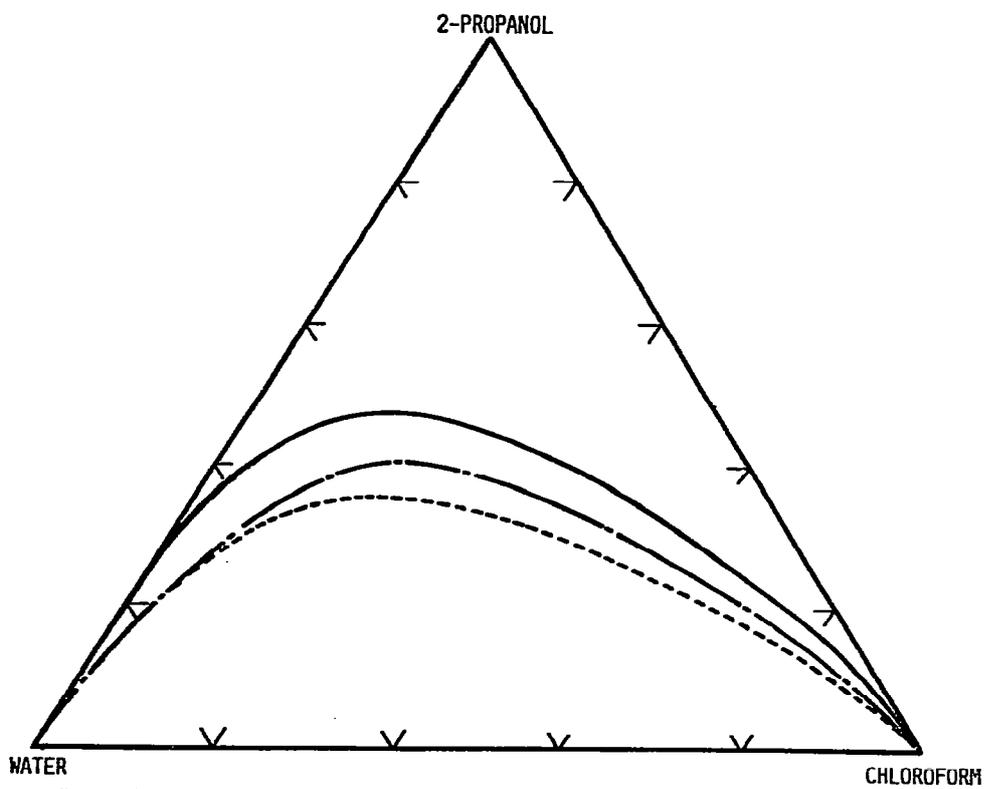


Fig. 7. Liquid-liquid equilibria for water-2-propanol-chloroform at 25°C [60]. ---, Effective UNIFAC; ·-·-·, UNIFAC; —, experimental.

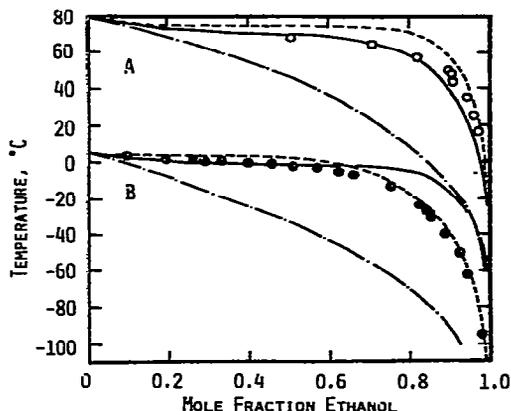


Fig. 8. Solid-liquid equilibria. Experimental: (A) ethanol-naphthalene,  $\circ$ , Sunier [62]; (B) ethanol-benzene,  $\bullet$ , Viala [63]. Calculated: —, effective UNIFAC; - - -, UNIFAC; - · - ·, ideal.

In solid-solubility calculations, enthalpies of fusion and melting temperatures for the solids studied in this work are taken from the literature [15,61]. Figure 8 shows temperature-composition diagrams for the ethanol-naphthalene and ethanol-benzene systems. In the ethanol-naphthalene system, effective UNIFAC gives calculated results closer to experimental data than UNIFAC [64]. However, for the ethanol-benzene system,

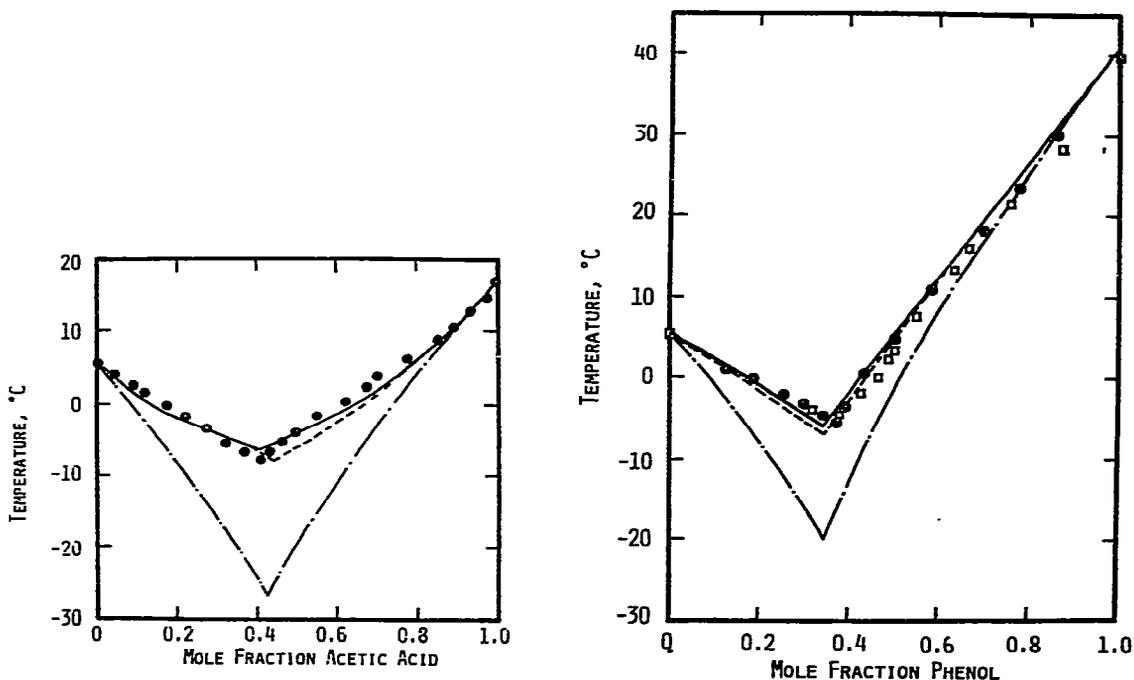


Fig. 9. Solid-liquid equilibria for acetic acid-benzene.  $\bullet$ , Experimental data of Tan et al. [69]. Calculated: —, effective UNIFAC; - - -, UNIFAC; - · - ·, ideal.

Fig. 10. Solid-liquid equilibria for benzene-phenol. Experimental:  $\bullet$ , Tsakalotos and Guye [70];  $\square$ , Hatcher and Skirrow [71]. Calculated: —, effective UNIFAC; - - -, UNIFAC; - · - ·, ideal.

TABLE 8  
Calculated and experimental eutectics in binary systems

System (component 1—component 2)	Mole% of component I			Temp. (°C)		
	I <sup>a</sup>	II <sup>b</sup>	Exptl. [60]	I	II	Exptl. [60]
Acetone—diethyl ether	32.0	34.0	24.0	-123	-123	-126
Acetone—ethanol	24.4	22.4	21.0	-124	-122	-119
Benzene—1,2-dichloroethane	31.6	30.6	32.0	-55	-56	-55
Benzene—phenol	65.4	65.8	62.5	-7	-6	-6
Benzene—1,4-dioxane	56.9	57.4	56.5	-26	-25	-26
Benzene—acetonitrile	12.6	3.4	5.0	-49	-45	-51
Benzene—cyclohexane	26.6	28.0	26.5	-48	-50	-44
Benzene—nitrobenzene	51.7	49.4	50.0	-27	-23	-26
Phenol—naphthalene	83.7	81.1	83.8	30	27	29
Acetic acid—benzene	44.6	40.9	40.9	-8	-7	-8
Acetic acid—cyclohexane	7.4	9.8	7.4	-6	-8	-1

<sup>a</sup> I = UNIFAC.

<sup>b</sup> II = Effective UNIFAC.

UNIFAC works much better. Table 7 presents solubilities for naphthalene, anthracene, and phenanthrene in different solvents. Figures 9 and 10 show two eutectic systems where UNIFAC and effective UNIFAC predict the experimental eutectic composition and eutectic temperature well. Calculated and experimental eutectic compositions and eutectic temperatures are listed for 11 binary systems in Table 8. Both methods give generally good agreement with experiment.

#### SIMULTANEOUS CORRELATION OF VAPOR—LIQUID EQUILIBRIA AND EXCESS ENTHALPY DATA

In the estimation of excess enthalpies with group-contribution methods, it has been found that a set of group parameters required for reproducing experimental excess enthalpy data are different from that used for activity coefficients [72,73]. Two recent investigations [74,75] were attempted to find a unique set of parameters which are able to reproduce activity coefficients and excess enthalpies simultaneously. Skjold-Jørgensen et al. [74] presented the modified UNIFAC model suited for the representation of mixtures containing non-associating components. Ashraf and Vera [75] tested SIGMA (Simplified Group Method Analysis) for the prediction of both data for alkane, alcohol, and chloroalkane systems. In this section, we will compare the ability of the effective UNIFAC method with that of SIGMA in the simultaneous representation of these two thermodynamic properties.

The Gibbs—Helmholtz equation provides the thermodynamic relation between excess enthalpy and activity coefficients.

$$-h^E/RT^2 = \sum_i x_i \partial \ln \gamma_i / \partial T \quad (17)$$

The basic equation of the effective UNIFAC may be given by

$$h^E = \sum_i x_i \sum_k \nu_{ki} (H_k - H_k^{(i)}) \quad (18)$$

with

$$\frac{H_k}{RT^2} = -\frac{\partial \ln \Gamma_k}{\partial T} = \sum_m X_m \eta_{mk} / \sum_m X_m \psi_{mk} + \sum_m \left( X_m \eta_{km} / \sum_n X_n \psi_{nm} \right) - \sum_m \left[ X_m \psi_{km} \left( \sum_n X_n \eta_{nm} \right) / \left( \sum_n X_n \psi_{nm} \right)^2 \right] \quad (19)$$

where

$$\eta_{nm} = \partial \psi_{nm} / \partial T \quad (20)$$

The group parameters  $a_{mn}$  are considered to be temperature-dependent.

$$a_{mn} = A_{mn}T + B_{mn} \quad (21)$$

Then

$$\eta_{mn} = \psi_{mn} B_{mn} / T^2 \quad (22)$$

Table 9 lists the coefficients  $A_{mn}$  and  $B_{mn}$ , which were obtained according to the procedure described by Ashraf and Vera [75]. Root-mean square relative deviations (percent) between experimental and calculated pressures and excess enthalpies for the reference systems studied in this work are given in Table 10 together with the values obtained using SIGMA coefficients. Excess enthalpies and total pressures for ternary systems including all three groups, CH<sub>2</sub>, CCOH, and CCl, are predicted and compared with literature values and the values by SIGMA in Table 11. It may be stated that the results obtained by effective UNIFAC are comparable with those by SIGMA for the systems tested here.

In conclusion, the practical utility of effective UNIFAC has been demonstrated. Omissions in the group-parameter table show where new reliable experimental data are necessary. The effective UNIFAC method will be revised as new phase equilibrium data become available. Further modifications of the present group-contribution method will contain the modified combinatorial expression suggested by Kikic et al. [81].

TABLE 9

Effective UNIFAC coefficients evaluated for prediction of both activity coefficients and excess enthalpies

$m/n$	$a_{mn}$ at 25°C	$A_{mn}$	$B_{mn}$ (K)
CH <sub>2</sub> /CCOH	1081.0	-1.292	1466.0
CCOH/CH <sub>2</sub>	143.7	0.135	103.4
CH <sub>2</sub> /CCl	278.1	-0.746	500.6
CCl/CH <sub>2</sub>	27.77	0.061	9.400
CCOH/CCl	167.6	-0.022	174.2
CCl/CCOH	641.1	-2.315	133.1

TABLE 10

Predicted results of vapor-liquid equilibria and excess enthalpies for binary systems

System	T (°C)	Data type	No. of data points	Root-mean square relative deviation (%)		Ref.
				SIGMA	Effective UNIFAC	
<i>n</i> -Heptane-1-propanol	25	V <sup>a</sup>	11	2.8	4.5	76
<i>n</i> -Heptane-1-propanol	30	V	9	2.9	2.6	77
<i>n</i> -Hexane-ethanol	55	V	17	4.5	3.8	78
<i>n</i> -Heptane-ethanol	40	V	10	8.2	6.6	22
<i>n</i> -Heptane-1-chlorobutane	25	V	11	0.6	0.5	76
1-Propanol-1-chlorobutane	25	V	15	1.5	1.1	76
<i>n</i> -Heptane-1-butanol	30	H <sup>b</sup>	11	8.5	6.6	77
<i>n</i> -Hexane-1-octanol	25	H	10		9.7	79
<i>n</i> -Hexane-2-chlorobutane	25	H	19	2.8	1.0	80
<i>n</i> -Octane-2-chlorobutane	25	H	19	1.4	1.9	80
1-Heptanol-1-chlorobutane	25	H	19	5.1	3.2	80
1-Octanol-1-chlorobutane	25	H	19	5.0	2.6	80

<sup>a</sup> V = vapor-liquid equilibria and deviation means pressure.<sup>b</sup> H = excess enthalpy.

TABLE 11

Predicted results of vapor-liquid equilibria and excess enthalpies for ternary systems at at 25°C

System	Data type	No. of data points	Root-mean square relative deviation (%)		Ref.
			SIGMA	Effective UNIFAC	
<i>n</i> -Hexane(1)-1-octanol(2)-1- chlorobutane(3)					79
( $x_2/x_3$ ) = 0.993	H <sup>a</sup>	10	3.5	7.4	
( $x_1/x_3$ ) = 1.000	H	10	8.0	5.3	
( $x_1/x_2$ ) = 1.007	H	10	4.5	7.6	
<i>n</i> -Heptane-1-propanol-1- chlorobutane	V <sup>b</sup>	44	2.6	2.1	76

<sup>a</sup> H = excess enthalpy.<sup>b</sup> V = vapor-liquid equilibria and deviation means pressure.

## ACKNOWLEDGEMENT

The authors wish to thank Dr. J.G. Gmehling of the University of Dortmund for supplying computer programs for solid-liquid equilibria using the UNIFAC method.

## REFERENCES

- 1 G.M. Wilson and C.H. Deal, *Ind. Eng. Chem. Fundam.*, 1 (1962) 20.
- 2 E.L. Derr and C.H. Deal, *I. Chem. E. Symp. Ser. No. 32 (Instn. Chem. Engrs. London) 1969, Session 3, p. 40.*
- 3 K. Kojima and K. Tochigi, *Prediction of Vapor-Liquid Equilibria by the ASOG Method*, Elsevier, Amsterdam, 1979.
- 4 Aa. Fredenslund, R.L. Jones and J.M. Prausnitz, *AIChE J.*, 21 (1975) 1086.
- 5 Aa. Fredenslund, J. Gmehling and P. Rasmussen, *Vapor-Liquid Equilibria using UNIFAC*, Elsevier, Amsterdam, 1977.
- 6 Aa. Fredenslund, J. Gmehling, M.L. Michelsen, P. Rasmussen and J.M. Prausnitz, *Ind. Eng. Chem. Process Des. Develop.*, 16 (1977) 450.
- 7 U. Onken and J. Gmehling, *Chem. Ing. Tech.*, 49 (1977) 404.
- 8 J. Gmehling and U. Onken, *Ber. Bunsenges. Phys. Chem.*, 81 (1977) 1023.
- 9 S. Skjold-Jørgensen, B. Kolbe, J. Gmehling and P. Rasmussen, *Ind. Eng. Chem. Process Des. Develop.*, 18 (1979) 714.
- 10 J. Gmehling, P. Rasmussen and Aa. Fredenslund, *Chem. Ing. Tech.*, 52 (1980) 724.
- 11 D.S. Abrams and J.M. Prausnitz, *AIChE J.*, 21 (1975) 116.
- 12 I. Nagata and K. Katoh, *Fluid Phase Equilibria*, 5 (1981) 225.
- 13 A. Bondi, *Physical Properties of Molecular Crystals, Liquids, and Glasses*, Wiley, New York, 1968.
- 14 J. Gmehling and U. Onken, *Vapor-Liquid Equilibrium Data Collection, DECHEMA Chemistry Series, Frankfurt/M, Vol. 1, Part 1, 1977, Part 2a, 1977, Part 2b, 1978 (together with W. Arlt), Part 3 + 4, 1979 (together with W. Arlt).*
- 15 J.A. Riddick and W.B. Bunger, *Organic Solvents*, Wiley-Interscience, New York, 1970, 3rd edn.
- 16 I. Wichterle, J. Linek and E. Hála, *Vapor-Liquid Equilibrium Data Bibliography*, Elsevier, Amsterdam, 1973, Supplement I, 1976, Supplement II, 1979.
- 17 J.M. Prausnitz, *Molecular Thermodynamics of Fluid Phase Equilibria*, Prentice-Hall, Englewood Cliffs, N.J., 1969.
- 18 J.G. Hayden and J.P. O'Connell, *Ind. Eng. Chem. Process Des. Develop.*, 14 (1975) 209.
- 19 J.M. Sorensen, T. Magnussen, P. Rasmussen and Aa. Fredenslund, *Fluid Phase Equilibria*, 3 (1979) 47.
- 20 H. Wolff and H.E. Höppel, *Ber. Bunsenges. Phys. Chem.*, 72 (1968) 710.
- 21 G.W. Lindberg and D. Tassios, *J. Chem. Eng. Data*, 16 (1971) 52.
- 22 G.A. Ratcliff and K.C. Chao, *Can. J. Chem. Eng.*, 47 (1969) 148.
- 23 L. Boublikova and B.C.Y. Lu, *J. Appl. Chem. (London)*, 19 (1969) 89.
- 24 I. Brown, W. Fock and F. Smith, *J. Chem. Thermodyn.*, 1 (1969) 273.
- 25 H.C. Van Ness, C.A. Soczek, G.L. Peloguin and R.L. Machado, *J. Chem. Eng. Data*, 12 (1967) 217.
- 26 L.L. Lee and W.A. Scheller, *J. Chem. Eng. Data*, 12 (1967) 497.
- 27 E. Neau, C. Blanc and D. Bares, *J. Chim. Phys. Physicochim. Biol.*, 70 (1973) 843.
- 28 I. Brown and F. Smith, *Austral. J. Chem.*, 12 (1959) 407.
- 29 G. Scatchard, S.E. Wood and J.M. Mochel, *J. Am. Chem. Soc.*, 68 (1946) 1957.
- 30 M. Benedict, C.A. Jonson, E. Solomon and L.C. Lubin, *Trans. Am. Inst. Chem. Engrs.*, 41 (1945) 371.
- 31 A.Ja. Aarna and T.K. Kaps, *Trudy Tallinskovo Politech. Inst. Ser. A*, 285 (1970) 3.
- 32 D. Tassios and M. Van Winkle, *J. Chem. Eng. Data*, 12 (1967) 555.
- 33 T.Ch. Lo, H.H. Bieber and A.E. Karr, *J. Chem. Eng. Data*, 7 (1962) 327.
- 34 H. Renon, *Int. Data Ser. A*, (1973) 67.
- 35 T. Tresczanowicz, *Bull. Acad. Polon. Ser. Sci. Chim.*, 11 (1973) 107.
- 36 I. Brown and F. Smith, *Austral. J. Chem.*, 10 (1957) 423.
- 37 J. Kraus and J. Linek, *Collect. Czech. Chem. Commun.*, 36 (1971) 2547.
- 38 I. Nagata, T. Ohta and T. Takahashi, *J. Chem. Eng. Jpn.*, 6 (1973) 129.
- 39 I. Matsunaga and T. Katayama, *J. Chem. Eng. Jpn.*, 6 (1973) 397.
- 40 J.L. Humphrey and M. Van Winkle, *J. Chem. Eng. Data*, 12 (1967) 526.

- 41 H. Wolff and H.E. Höppel, *Ber. Bunsenges. Phys. Chem.*, 70 (1966) 874.
- 42 G. Schneider, *Z. Phys. Chem., N.F.*, 24 (1960) 165.
- 43 T.M. Letcher and J.W. Bayles, *J. Chem. Eng. Data*, 16 (1971) 266.
- 44 I. Brown and F. Smith, *Austral. J. Chem.*, 8 (1955) 62.
- 45 I. Brown and F. Smith, *Austral. J. Chem.*, 8 (1955) 501.
- 46 L.S. Kudryvtseva and M.P. Susarev, *Zh. Prikl. Khim.*, 36 (1963) 1231.
- 47 J. Sameshima, *J. Am. Chem. Soc.*, 40 (1918) 1482.
- 48 E. Sada and T. Morisue, *J. Chem. Eng. Jpn*, 8 (1975) 191.
- 49 T. Ito and F. Yoshida, *J. Chem. Eng. Data*, 8 (1963) 315.
- 50 H. Sugi and T. Katayama, *J. Chem. Eng. Jpn*, 11 (1978) 167.
- 51 V. Klement, V. Fried and J. Pick, *Collect. Czech. Chem. Commun.*, 29 (1964) 2008.
- 52 P.O. Haddad and W.C. Edmister, *J. Chem. Eng. Data*, 17 (1972) 275.
- 53 A.E. Karr, E.G. Scheibel, W.M. Bowes and D.F. Othmer, *Ind. Eng. Chem.*, 43 (1951) 961.
- 54 I. Nagata, *J. Chem. Eng. Data*, 7 (1962) 367.
- 55 H.W. Schulte, *Diplomarbeit, Universität Dortmund*, 1974.
- 56 J.G. Dunlop, *M.S. thesis, Brooklyn Polytech. Inst.*, 1948.
- 57 T. Ohta, J. Koyabu and I. Nagata, *Fluid Phase Equilibria*, in press.
- 58 A. Palmer and B.D. Smith, *J. Chem. Eng. Data*, 17 (1972) 71.
- 59 I. Mertl, *Collect. Czech. Chem. Commun.*, 37 (1972) 366.
- 60 Landolt-Börnstein, *Zahlenwerte und Funktionen aus Physik, Chemie, Astronomie, Geophysik und Technik, Vol. II, part 2c*, Springer-Verlag, Berlin, 1964, 6th edn.
- 61 Landolt-Börnstein, *Zahlenwerte und Funktionen aus Physik, Chemie, Astronomie, Geophysik und Technik, Vol. II, part 4*, Springer-Verlag, Berlin, 1961, 6th edn.
- 62 A. Sunier, *J. Phys. Chem.*, 34 (1930) 2532.
- 62 F. Viala, *Bull. Soc. Chim. Fr.*, 15 (1914) 5.
- 64 J.G. Gmehling, T.F. Anderson and J.M. Prausnitz, *Ind. Eng. Chem. Fundam.*, 17 (1978) 269.
- 65 H. Ward, *J. Phys. Chem.*, 30 (1926) 1316.
- 66 J. Hildebrand and C.A. Jenks, *J. Am. Chem. Soc.*, 42 (1920) 2180.
- 67 J. Fohl, M. Fris and M. Smutek, *Collect. Czech. Chem. Commun.*, 31 (1966) 4015.
- 68 H. Henstock, *J. Chem. Soc.*, 121 (1922) 2124.
- 69 W. Tan, K.A. Kriger and J.G. Miller, *J. Am. Chem. Soc.*, 74 (1952) 6181.
- 70 D. Tsakalotos and P. Guye, *J. Chim. Phys.*, 8 (1910) 340.
- 71 W. Hatcher and F. Skirrow, *J. Am. Chem. Soc.*, 39 (1917) 1939.
- 72 T.H. Nguyen and G.A. Ratcliff, *Can. J. Chem. Eng.*, 52 (1974) 641.
- 73 I. Nagata and T. Ohta, *Chem. Eng. Sci.*, 33 (1978) 177.
- 74 S. Skjold-Jørgensen, P. Rasmussen and Aa. Fredenslund, *Chem. Eng. Sci.*, 35 (1980) 289.
- 75 F.A. Ashraf and J.H. Vera, *Fluid Phase Equilibria*, 4 (1980) 211.
- 76 S.G. Sayegh, J.H. Vera and G.A. Ratcliff, *Can. J. Chem. Eng.*, 57 (1979) 513.
- 77 S.G. Savini, D.R. Winterhalter and H.C. Van Ness, *J. Chem. Eng. Data*, 10 (1965) 168.
- 78 J.C.K. Ho and B.C.Y. Lu, *J. Chem. Eng. Data*, 8 (1963) 549.
- 79 T.T. Lai, T.H. Doan-Nguyen, J.H. Vera and G.A. Ratcliff, *Can. J. Chem. Eng.*, 56 (1978) 358.
- 80 T.H. Nguyen and G.A. Ratcliff, *J. Chem. Eng. Data*, 20 (1975) 256.
- 81 I. Kikic, P. Alessi, P. Rasmussen and Aa. Fredenslund, *Can. J. Chem. Eng.*, 58 (1980) 253.